

Microarrays

 A tool for capturing genetic information (genotype, gene expression etc.) at a large scale

Nov 14, 2014

Using high-throughput genotype data to answer questions on complex diseases (Sham & Cherney, 2011)

- Genetic variants involved in individual differences in the propensity to develop disease
- Where are these sequence changes located on the 23 chromosomes that constitute the human genome?
- What is the nature of the sequence changes in these variants (e.g., single base pair changes, copy number changes, etc.)?

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Questions ...

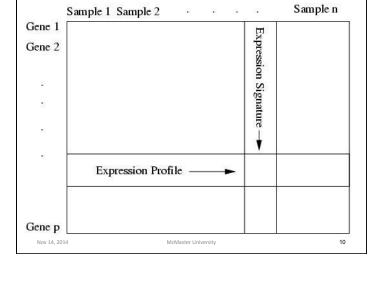
- What are the frequencies and effect sizes of these changes?
- How important are these changes relative to the environmental variation in explaining individual differences in disease susceptibility?
- And how do the genetic changes interact with each other and with environmental factors?

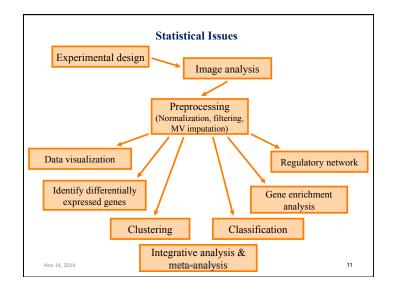
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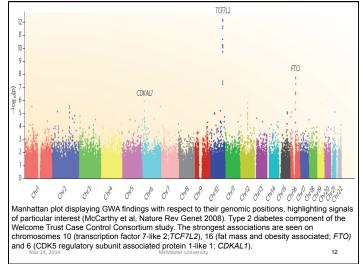
Applications of Microarray Technology

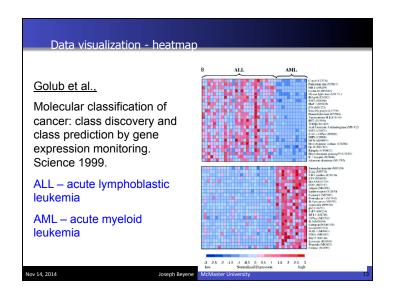
- Gene expression profiling
 - · In different cells/tissues
 - During the course of development
 - Under different environmental or chemical stimuli
 - In disease state versus healthy
- Molecular diagnosis:
 - Molecular classification of diseases
- Drug development
 - Identification of new targets
- Pharmacogenomics
 - · Individualized medicine

The "Omics" era Genome – genomics Epigenomics Phrmacogenomics Nutrigenomics Transcriptome - transcriptomics Protein – proteomics Metabolome – metabolomics Interactomics etc











"Biostatomics"

- The <u>art</u> and <u>science</u> of extracting, organizing, analyzing and interpreting "omics", clinical, lifestyle and other environmental data
 - systemizing diverse data in order to produce useful information
- A crucial tool for an interdisciplinary research on the determinants and impact of complex diseases:
 - molecular-genetic factors, risk modifiers and population health

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Why integrate data?

- Class comparison/univariate association
 - Improve power to measure small effects
 - Improve precision of estimated effects
 - Assess heterogeneity
- Association/correlation between different sets of variables
 - derive structure in each set and maximize their correlation
- Class prediction
 - Improve prediction accuracy
 - Understand (quantify) relative contribution of different sources of data

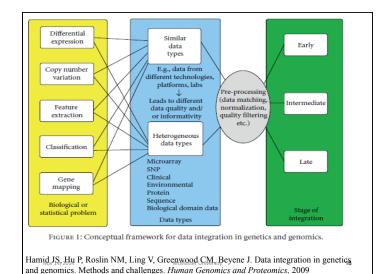
Data integration

- Conceptual framework
- Integrating similar data types
- Integrating heterogeneous data types
- Integrating statistical information with biological domain data

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Part-1:
Class comparison / univariate
association

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Integrating "Similar" Data

- Meta-analysis approaches and methods
 - Fixed versus random effect models
 - Weights based on quality scores
 - Different parameterization of association parameter (i.e., different effect size)
 - Modified meta-analytic methods for heterogeneous cohorts

Integrating "similar" data types

- Meta-analytic techniques have been used with excellent success to combine similar types of data across different studies that address similar hypotheses
- We have demonstrated that our ability to detect associations can be greatly enhanced when proper meta-analytic techniques are applied

Hu, P., Greenwood, C.M.T., Beyene, J. (2005). Integrative analysis of multiple gene expression profiles with quality-adjusted effect size models. *BMC Bioinformatics*, vol. 6, 128, pp. 1–11.

Hu P, Greenwood CM, Beyene J. Using the ratio of means as the effect size measure in combining results of microarray experiments. BMC Syst Biol. 2009, 5;3:106. Neupane B, Loeb M, Anand SS, Beyene J. Meta-analysis of genetic

association studies under heterogeneity. Eur J Hum Genet. 2012, 11:1174-81.

Friedrich JO, Adhikari NKJ, Beyene J. Ratio of geometric means to analyze continuous outcomes in meta-analysis: comparison to mean differences and ratio of arithmetic means using empiric data and simulation. Stat Med. 2012

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Hypotheses

- \diamond Suppose there are k cohorts (studies/populations)
- let the effect in i^{th} cohort = β_i
- **❖** Fixed effect model
 - **!** (Traditional) FE: H_0 : $\beta_1 = ... = \beta_k = \beta = 0$ vs. H_1 : $\beta_1 = ... = \beta_k = \beta \neq 0$
 - New FE: H_0 : $\beta_1 = ... = \beta_k = 0$ vs. H_1 : $\beta_i \neq 0$ for at least one cohort
- * Random effect model:

Let $\beta_1, \beta_2, ..., \beta_k \sim \text{iid N}(\mu, \tau^2)$; $\mu = \text{overall mean}, \tau^2 = \text{between-cohort variance}$

- **\(\text{(Traditional) RE: } \(H_0: \mu = 0 \) vs. H_1: \mu \neq 0.**
- New RE: H_0 : $\mu = 0$ and $\tau^2 = 0$ vs. H_1 : $\mu \neq 0$ or $\tau^2 > 0$

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22

Test statistics

- Let $\hat{\beta}_i$ and s_i be the estimate of β_i and it SE in the *i*th cohort
- * Fixed effect model
 - **FE:** $T = (\Sigma_i w_i \hat{\beta}_i)^2 / \Sigma_i w_i \sim \chi_1^2$; where $w_i = 1/s_i^2$
 - New FE: $T = \Sigma_i (\hat{\beta}_i / s_i)^2 \sim \chi_k^2$
- Random effect model:

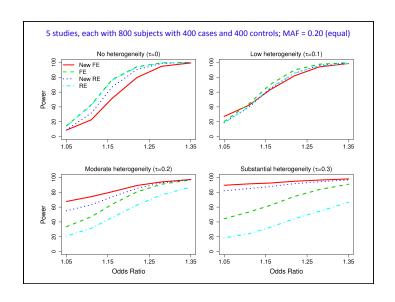
Obtain $\hat{\tau}^2$, $\hat{\mu} = \sum_i w_i \hat{\beta}_i / \sum_i w_i$; $var(\hat{\mu}) = 1/\sum_i w_i$; where $w_i = 1/(s_i^2 + \hat{\tau}^2)$

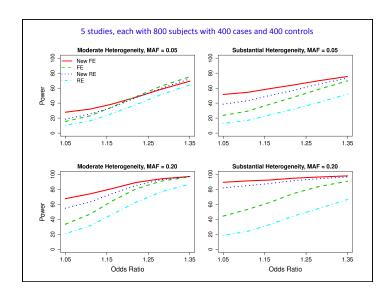
- RE: Wald test, $T = \widehat{\mu}^2 / var(\widehat{\mu}) \sim \gamma_1^2$
- New RE: LR test, $T = 2(l(\hat{\mu}, \hat{\tau}^2) l(0, 0)) \sim (\chi_1^2 + \chi_2^2)/2$

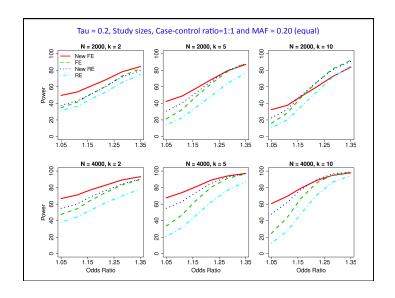
Simulation Study

- \Leftrightarrow Genotypes, x = 0, 1, 2
- ❖ Total sample sizes, N: 2000, 4000, 6000, 8000, 10000
- ❖ Number of studies, k: 2, 3, 5, 7, 10 studies
- $\beta_1, \beta_2, ..., \beta_k$ were simulated from $N(\mu, \tau^2)$
- 10,000 simulations for each combination of (μ, τ) , where
- > Average effect, μ=0, .05, .10, .15, .20, .25, .30
- Corresponding ORs: 1.00, 1.05, 1.11, 1.16, 1.22, 1.28, 1.35.
- \triangleright Heterogeneity, $\tau = 0, 0.1, 0.2, 0.3$
- ❖ SNPs minor allele frequency (MAF): MAF = 0.05; MAF = 0.20
- ❖ Genetic risk models: Multiplicative, Dominant, Recessive
- Data were simulated/analyzed using logistic regression

Neupane B, Loeb M, Anand SS, Beyene J. Meta-analysis of genetic association studies under neterogeneity. Eur J Hum Genet. 2012. 17117174-81.







Integrating "heterogeneous" data

- Observations for different types of variables are available on the same subjects in each study
 - Example-1:
 - Sparse canonical correlation analysis (SCCA)
 - Example-2:
 - Weighted Kernel Fisher discriminant analysis (wKFDA)

Part-II Correlation across data types

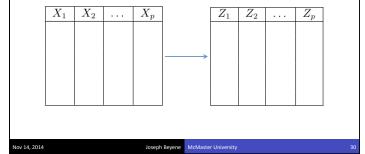
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Classical PCA Review

• Transform the original variables into new set of variables called principal components.



Classical PCA Review

 Principal components are nothing but linear combinations of the original variables:

$$(PC 1) \quad Z_1 = v_{11}X_1 + v_{12}X_2 + \dots + v_{1p}X_p = \mathbf{v}_1'\mathbf{X}$$

$$(PC\ 2) \quad Z_2 = v_{21}X_1 + v_{22}X_2 + \dots + v_{2p}X_p = \mathbf{v}_2'\mathbf{X}$$

$$(PC \ p) \quad Z_p = v_{p1}X_1 + v_{p2}X_2 + \dots + v_{pp}X_p = v_p' \mathbf{X}$$

• Loading values: $V = (v_1, v_2, \dots, v_p)$

Nov. 14, 2017

seph Beyene

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Classical PCA Review

- Three identifying properties:
 - 1. **Maximized Variances:** $Var(Z_1) \ge Var(Z_2) \ge ... \ge Var(Z_p) \ge 0$.
 - 2. Orthonormal Loading Vectors, Uncorrelated PCs: $\|\mathbf{v}_j\|_2^2 = 1$, $\mathbf{v}_j'\mathbf{v}_m = 0$ and $Cov(Z_j, Z_m) = 0$ for $j \neq m$.
 - 3. **Total Variance preserved:** $\sum_{j=1}^{p} Var(Z_j) = \sum_{j=1}^{p} Var(X_j)$.
- Variance-covariance matrix dictates solutions.
- Easily found with SVD: X = UDV'

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Issues in High-dimensional data

• All non-zero loadings; cannot interpret.

$$(PC\ 1)$$
 $Z_1 = -0.56X_1 - 0.59X_2 - 0.57X_3 + 0.07X_4 + 0.02X_5 - 0.01X_6 + .$

$$(PC\ 2)$$
 $Z_2 = 0.01X_1 + 0.10X_2 - 0.04X_3 + 0.77X_4 - 0.63X_5 + 0.01X_6 + \dots$

$$(PC\ 3)$$
 $Z_3 = 0.61X_1 - 0.14X_2 - 0.51X_3 - 0.38X_4 - 0.44X_5 - 0.01X_6 + \dots$

$$(PC \ 4) \quad Z_4 = 0.47X_1 - 0.72X_2 + 0.32X_3 + 0.31X_4 + 0.25X_5 - 0.02X_6 + \dots$$

$$(PC 5)$$
 $Z_5 = 0.29X_1 + 0.32X_2 - 0.56X_3 + 0.40X_4 + 0.58X_5 + 0.06X_6 + \dots$

$$(PC 6) \quad Z_6 = 0.05X_1 - 0.05X_2 - 0.01X_3 - 0.07X_4 - 0.07X_5 + 0.99X_6 + \dots$$

• Unrealistic and impractical for latent features of the data to be driven by so many variables.

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Sparse PCA

• Force those small residual loadings to 0

$$(PC\ 1) \quad Z_1 = -0.72X_1 - 0.60X_2 - 0.35X_3 + 0X_4 + 0X_5 - 0X_6$$

$$(PC\ 2) \quad Z_2 = 0X_1 + 0X_2 + 0X_3 - 0.67X_4 + 0.74X_5 + 0X_6$$

$$(PC\ 3)\quad Z_3=-0.27X_1-0.22X_2+0.94X_3+0X_4+0X_5+0X_6$$

$$(PC\ 4)$$
 $Z_4 = 0.64X_1 - 0.77X_2 + 0X_3 + 0X_4 + 0X_5 + 0X_6$

$$(PC 5) \quad Z_5 = 0X_1 + 0X_2 + 0X_3 - 0.74X_4 - 0.67X_5 + 0X_6$$

$$(PC 6) \quad Z_6 = 0X_1 + 0X_2 + 0X_3 + 0X_4 + 0X_5 + 1X_6$$

• Introduce sparseness to the loadings through adjusting tuning parameters

Extensive Simulation

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Sparse Principal Component Analysis for High-Dimensional Data: A Comparative Study

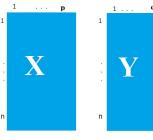
Ashley J. Bonner

McMaster University, ashleybonner8@email.con

http://digitalcommons.mcmaster.ca/cgi/viewcontent.cgi? article=8155&context=opendissertations

Canonical Correlation

• Consider two datasets with p and q variables, obtained on n observations.



Example-1 CCA: Cardiac Surgery Data

$$X = \begin{pmatrix} x_1 & x_2 & \dots & x_p & & y_1 & y_2 & \dots & y_q \\ x_{11} & x_{12} & \dots & x_{1p} & & & & \\ & \ddots & & & & \\ x_{n1} & x_{n2} & \dots & x_{np} \end{pmatrix} \qquad Y = \begin{pmatrix} y_{11} & y_{12} & \dots & y_{1q} \\ & \ddots & & & \\ y_{n1} & y_{n2} & \dots & y_{nq} \end{pmatrix}$$

- Need to find relationship between risk factors and various outcomes in cardiac surgery
- n = 2605 patients who underwent cardiac surgery
- p = 74 potential risk factors
- q = 12 different outcome measures

Ridderstople et al. Canonical correlation analysis of risk factors and clinical outcomes in cardiac surgery, Journal of Medical Systems, 2005

CCA ...

- Need samples at least 20 x number of variables to avoid computational problems and to estimate parameters accurately
- Solutions are linear combinations of entire sets of variables under consideration
- In high-dimensional data, sample size is very small compared to number of variables

Barcikowski and Stevens. A Monte Carlo study of stability of canonical correlations, canonical weights and canonical variate-variable correlations. Multivariate Behavioral Research, 1975

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Canonical Correlation Analysis

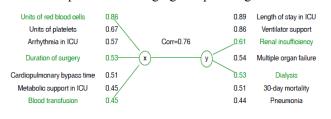
- Canonical correlation analysis (CCA) is a classical multivariate method used for finding correlations between two sets of multi-dimensional variables.
 - CCA can be used for dimension reduction and data visualization.
- maximize_{a,b} a'X'Yb subject to a'X'Xa = 1, b'Y'Yb = 1
- CCA gives a linear combination of X that is highly associated with a linear combination of Y measurements

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Sparse canonical correlation analysis

- Automated selection of variables based on mathematical objective function
- Developed fast-converging computer algorithm



E Parkhomenko, D. Tritchler, J. Beyene .Sparse Canonical Correlation Analysis with Application to Genomic Data Integration. Statistical Applications in Genetics and Molecular Biology, 2009

SCCA – a comparison of methods (Sathish Pichika's MSc project)

- We compared three SCCA methods: Parkhomenko et al. (2009), Witten et al. (2009), and Lee et al. (2011)
- In SCCA, only a sparse set of variables will be included in the solution from

maximize_{a,b} a'X'Yb

subject to $\mathbf{a}'\mathbf{a} \leq 1$, $\mathbf{b}'\mathbf{b} \leq 1$, $P_1(\mathbf{a}) \leq C_1$, $P_2(\mathbf{b}) \leq C_2$

- CCA/SCCA seeks weights a, b such that Cor(Xa, Yb) is large but in SCCA most of the weights are 0. i.e., a's, b's are 0.
- The penalty functions vary and tuning parameters estimated using cross-

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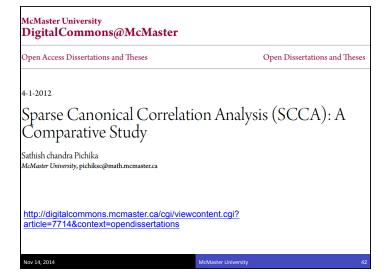
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Simulation

- Let X contain p variables and Y contains q variables and sample sizes be n.
- Suppose only a subset of variables in X is correlated with a subset of variables in Y
 - first few variables in X is highly correlated with the first few variables in Y

$$X = \begin{bmatrix} x_{11} & \cdots & x_{1r} & \cdots & x_{1p} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{n1} & \cdots & x_{nr} & \cdots & x_{np} \end{bmatrix} Y = \begin{bmatrix} y_{11} & \cdots & y_{1r} & \cdots & y_{1q} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ y_{n1} & \cdots & y_{nr} & \cdots & y_{np} \end{bmatrix}$$

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Parameters Varied in Simulation								
Varied Parameter	Description	Values between						
n	Observations	30 and 500						
p	Number of variables in X	50 and 2000						
q	Number of variables in X	30 and 1500						
r	Number of Correlated variables	5 and 50						
$\sigma_{\rm e}$	Std. Dev. of Latent variable (μ)	1.8 and 4						
σ_{μ}	Std. Dev. of nuisance variable	0.1 and 0.5						
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 Using the angle between the true canonical variates and their estimates as the measure of closeness (Johnstone and Lu (2009)) given by

$$dist(a_1, \hat{a_1}) = sin \angle (a_1, \hat{a_1}) = \sqrt{1 - (a_1^T \hat{a_1})^2}$$

- Discordance measures
 - number of false negatives (FNN) and false positives (FPN)
 - FP = number of nuisance variables with non-zero loadings in the resulting
 - FN = number of correlated variables with zero loadings in the resulting
- For each scenario, measures are averaged over 1000 simulated datasets

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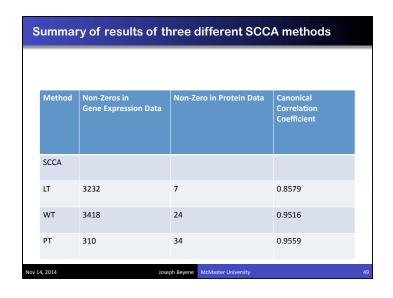
Table 1: n = 100, p = 300, q = 200, r = 15, σ_{μ} = 2, σ_{e} = 0.01 WT = Witten et al. (2009), LT = Lee et al. (2011), PT = Parkhomenko et al. (2009), CCA = Classical Canonical Correlation Analysis. Method CCA 0.9738 0.17 0.19 285 185 0 0 0.9975 0.09 0.09 0 0 2.75 2.55 WT 8.82 0.9935 0.21 0.20 3 0.36 6.91 0.02 0.02 0.63 0 0 0.9975 0.91 CCA 0.17 0 0.9741 0.17 285 185 0.9975 0.09 0.09 0 0 0 D WT 0.9930 0.19 0.18 0 0 11 0.9975 0.02 0.02 0 0 0 0 Nov 14, 2014

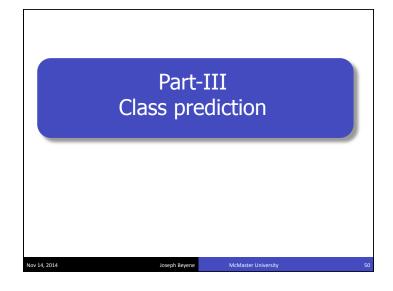
Method	r	Test Corr.	Dist (a)	Dist (b)	FPN (a)	FPN (b)	FNN (a)	FNN (b)
PT	5	0.7519	0.31	0.31	11.52	9.16	0.07	0.04
WT		0.75543	0.47	0.49	0.83	0.14	2.72	2.84
LT		0.7737	0.16	0.15	17	14	0.07	0.03
PT		0.7541	0.24	0.23	12.84	9.97	0.77	0.71
WT	15	0.7492	0.53	0.57	0.21	0	9.52	10.39
LT		0.7743	0.18	0.16	15.9	14	0.76	0.31

Application

- Gene and protein expression data were obtained from the National Cancer Institute http://discover.nci.nih.gov/cellminer/
 - The data contains 60 humans cancer cell lines that include a variety of cancer tissues of origins such as leukemias, lymphomas, and carcinomas of ovarian, renal, breast, prostate, colon, lung, and CNS origin
- Pre-processing (normalization, filtering) prior to applying SCCA methods
 - n = 59
 - X (gene expression data): p = 10,123
 - Y (protein data): q = 89

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Kernel-based statistical methods

- Reduce data to the same dimension and common format
 - Each data source is represented as a kernel matrix K_i
 - Kernels are similarity measures e.g., Gaussian and polynomial kernels
- Let $K = \{K1, K2,..., Km\}$ we can define a combined kernel as $\sum \mu_i K_i$,
- We proposed weights based on classification accuracy
- wKFD analysis is performed on the combined kernel

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Kernels

- Kernels will be of size n by n
- Any symmetric, positive semi-definite function is a valid kernel
- Linear, polynomial, Gaussian etc.

Hamid JS, Greenwood CMT, Beyene J. Weighted kernel Fisher discriminant analysis for integrating heterogeneous data. Comput Stat Data Anal., 2012, 56:2031–40.

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Weighted kernels

$$K = \sum_{i=1}^m w_i K_i,$$

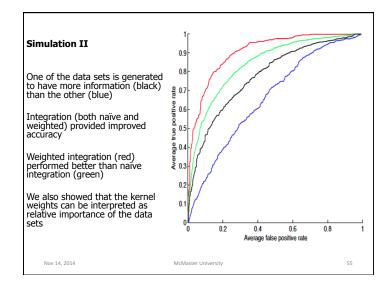
where w_i are given by

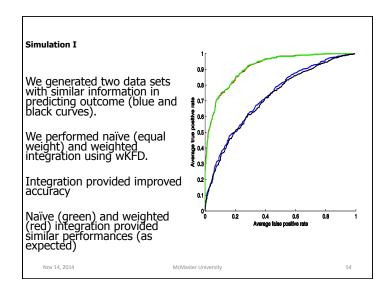
$$w_i = egin{cases} rac{1}{e_i} - 2, & ext{if } e_i \leq 0.5 \ 0, & ext{otherwise} \end{cases}$$

Hamid JS, Greenwood CMT, Beyene J. Weighted kernel Fisher discriminant analysis for integrating heterogeneous data. Comput Stat Data Anal., 2012, 56:2031-40.

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Illustrative example – integration of clinical and gene expression data in cancer prediction

- We used a publicly available breast cancer data set
- 295 breast cancer patients of whom 180 had poor prognosis (distant metastases) and 115 had good prognosis (free of distant metastases).
- Aim: Predict disease outcome (good or poor prognosis)

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AUC (se)

0.613 (0.054)

0.593 (0.049)

0.646 (0.051)

0.644 (0.053)

58

Error (se)

0.300 (0.038)

0.299 (0.038)

0.293 (0.042)

0.275 (0.039)

Illustrative example ...

- Clinical data consists of 12 variables age, number of positive nodes, tumor diameter, histologic grade, mastectomy, chemotherapy, hormonal therapy, NIH risk, Estrogen Receptor status, St Gallen recommendation, NIH recommendation, Tumor stage
- Gene expression data consists of 24, 479 genes
- We used IQR to filter gene expression data 214 genes were included in the analysis
- wKFD analysis was performed to estimate the relative importance of clinical and gene expression data in predicting disease outcome

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Clinical and gene expression data provided similar predictive accuracy

Equal weights are assigned to the clinical and gene expression data.

Clinical

0.5

0.4995 (0.015)

Method

KFD

KFD

wKFD (naive)"

Standard errors for the weights.

Integration of the two data sets provided little improvement, this may be due to data redundancy

Average standardized weights, classification error, and area under the ROC curve and their corresponding standard errors (se) for the breast cancer data

Gene expression

0.5005 (0.015)*

0.5

Weight

Both naïve and weighted integration provided similar performance

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Challenge

 Needle in the haystack problem Over fitting is a huge issue Biological validation is critical Nov 14, 2014

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CORRESPONDENCE



Retraction: A Genomic Strategy to Refine Prognosis in Early-Stage Non-Small-Cell Lung Cancer. N Engl J Med 2006;355:570-80.

TO THE EDITOR: We would like to retract our ar- Jason Koontz, M.D. ticle, "A Genomic Strategy to Refine Prognosis in Duke University Medical Center Early-Stage Non-Small-Cell Lung Cancer," which Durham, NC was published in the Journal on August 10, 2006. Robert Kratzke, M.D. Using a sample set from a study by the American University of Minnesota College of Surgeons Oncology Group (ACOSOG)

Minneapolis, MN and a collection of samples from a study by the Mark A. Watson, M.D., Ph.D. Cancer and Leukemia Group B (CALGB), we have Washington University School of Medicine tried and failed to reproduce results supporting the validation of the lung metagene model de- Michael Kelley, M.D. scribed in the article. We deeply regret the effect Geoffrey S. Ginsburg, M.D., Ph.D. of this action on the work of other investigators. Inivestigators university west, Ph.D.

St. Louis, MO

David H. Harpole, Ir., M.D.

Challenges ...

- The "curse" of technology
 - Capacity for collecting data has surpassed the data analysis techniques, and it is only getting worse with newer data types (e.g. whole genome sequence)
- Interdisciplinary collaboration is crucial for success
 - Basic biologists; clinicians; statisticians; computer scientists; mathematicians

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Conclusions ...

- New and efficient statistical methodologies need to be developed and validated
- Appropriate pre-processing of data, quality assessment and adjustment, biological validation etc. are crucial.

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Conclusions

- With the availability of many large-scale 'omics' data along with clinical and environmental data, integrative analysis is becoming crucial
 - can help unravel relationships between different biological functional levels
 - May lead to improved accuracy in the context of prediction
 - Allows detection of small effects sizes
 - Explore heterogeneity
- There are major computational and statistical challenges due to high-dimensional nature of data (e.g., large number of variables but small sample size)